

ENERGY: MOCK EXAM

① * First, let's determine the value of each force

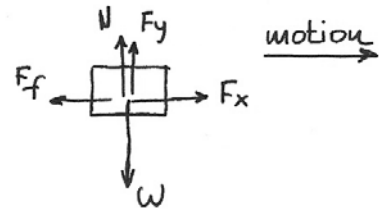
$$W = 500 \text{ kg} \times 10 \frac{\text{m}}{\text{s}^2} = 5000 \text{ N}$$

$$F_x = 1000 \text{ N} \times \cos 30^\circ = 866 \text{ N}$$

$$F_y = 1000 \text{ N} \times \sin 30^\circ = 500 \text{ N}$$

$$N + F_y = W \rightarrow N = W - F_y = 4500 \text{ N}$$

$$F_f = \mu \times N = 0.15 \times 4500 \text{ N} = 675 \text{ N}$$



* The work done by each force is:

$$W_w = 5000 \text{ N} \times 50 \text{ m} \times \cos 90^\circ = 0$$

$$W_F \begin{cases} W_F = 1000 \text{ N} \times 50 \text{ m} \times \cos 30^\circ = 43300 \text{ J} \\ W_{F_x} = 866 \text{ N} \times 50 \text{ m} \times \cos 0^\circ = 43300 \text{ J} \end{cases}$$

$$W_N = 4500 \text{ N} \times 50 \text{ m} \times \cos 90^\circ = 0$$

$$W_{F_f} = 675 \text{ N} \times 50 \text{ m} \times \cos 180^\circ = -33750 \text{ J}$$

* The total work is

$$\begin{aligned} W_{\text{TOTAL}} &= W_F + W_{F_f} + W_w + W_N = 43300 \text{ J} - 33750 \text{ J} = \\ &= 9550 \text{ J} \end{aligned}$$

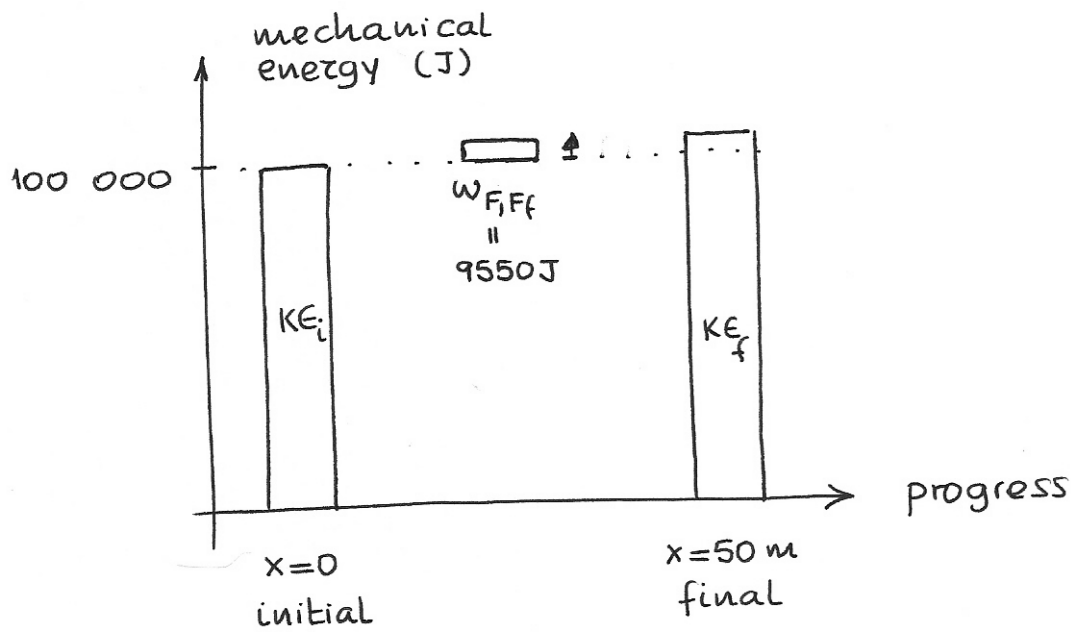
* The final velocity

$$W_{\text{TOTAL}} = \Delta KE \rightarrow W_{\text{TOTAL}} = KE_{\text{final}} - KE_{\text{initial}}$$

$$9550 \text{ J} = \frac{1}{2} \times 500 \text{ kg} \times v_f^2 - \frac{1}{2} \times 500 \text{ kg} \times \left(20 \frac{\text{m}}{\text{s}}\right)^2$$

$$9550 \text{ J} = 250 \text{ kg} \times v_f^2 - 100000 \text{ J}$$

$$v_f = \sqrt{\frac{109550 \text{ J}}{250 \text{ kg}}} \rightarrow v_f = 20.9 \frac{\text{m}}{\text{s}}$$



② a) The initial and final mechanical energies

$$E_i = PE_i + KE_i \rightarrow E_i = mgh = 10\text{kg} \times 10 \frac{\text{m}}{\text{s}^2} \times 20\text{m} = \boxed{2000\text{J}}$$

↑
initially at rest
 $v_0 = 0 \rightarrow KE_i = 0$

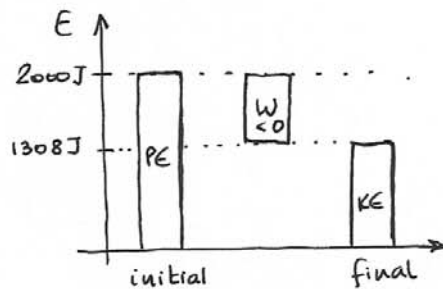
$$W_{F, F_f} = F_f \times d \times \cos 180^\circ = 17.3\text{N} \times 40\text{m} \times (-1) = \boxed{-692\text{J}}$$

$$\sin 30^\circ = \frac{h}{d}; d = 40\text{m}$$

$$F_f = \mu N = 0.2 \times 86.6\text{N} = 17.3\text{N}$$

$$N = W_y = W \times \cos 30^\circ = 86.6\text{N}$$

$$W_{F, F_f} = \Delta E = E_f - E_i \rightarrow -692\text{J} = E_f - 2000\text{J} \rightarrow \boxed{E_f = 1308\text{J}}$$



b) Final velocity

$$KE_f = 1308\text{J} = \frac{1}{2} \times 10\text{kg} \times v_f^2 \rightarrow \boxed{v_f = 16.2 \frac{\text{m}}{\text{s}}}$$

c) Acceleration

$$c1) F_{\text{net}} = m \cdot a \rightarrow -F_f + W_x = m \cdot a \rightarrow$$

$$\rightarrow -17.3\text{N} + 50\text{N} = 10\text{kg} \times a \rightarrow \boxed{a = 3.27 \frac{\text{m}}{\text{s}^2}}$$

$$c2) v_{\text{average}} = \frac{0 + 16.2\text{m/s}}{2} = 8.1 \frac{\text{m}}{\text{s}}$$

$$t = \frac{d}{v_{\text{av}}} = \frac{40\text{m}}{8.1\text{m/s}} = 4.94\text{s} \rightarrow a = \frac{\Delta v}{t} = \frac{16.2\text{m/s} - 0}{4.94\text{s}} \rightarrow$$

$$\rightarrow \boxed{a = 3.28 \frac{\text{m}}{\text{s}^2}}$$