

SOLUTIONS TO THE CONCEPTUAL TEST

1 $\Delta KE = -150 \text{ J}$

The values of kinetic energies are:

$$KE \text{ (final)} = 250 \text{ J}$$

$$KE \text{ (initial)} = 400 \text{ J}$$

Therefore, the change in kinetic energy is

$$\Delta KE = KE \text{ (final)} - KE \text{ (initial)} = -150 \text{ J}$$

2 $\Delta PE = 400 \text{ J}$

The values of potential energies are:

$$PE \text{ (final)} = 1250 \text{ J} - 250 \text{ J} = 1000 \text{ J}$$

$$PE \text{ (initial)} = 1000 \text{ J} - 400 \text{ J} = 600 \text{ J}$$

Therefore, the change in potential energy is

$$\Delta PE = PE \text{ (final)} - PE \text{ (initial)} = 400 \text{ J}$$

3 $\Delta E = 250 \text{ J}$

The values of mechanical energies are:

$$E \text{ (final)} = 1250 \text{ J}$$

$$E \text{ (initial)} = 1000 \text{ J}$$

Therefore, the change in mechanical energy is:

$$\Delta E = E \text{ (final)} - E \text{ (initial)} = 250 \text{ J}$$

Another way to calculate it is:

$$\Delta E = \Delta KE + \Delta PE = -150 \text{ J} + 400 \text{ J} = 250 \text{ J}$$

4 $W_{\text{total}} = -150 \text{ J}$

We can't calculate it using the definition of work: $W_{\text{total}} = F_{\text{net}} * d * \cos \alpha$, but from the work-energy theorem we can relate the total work done by all forces to the change in kinetic energy.

Therefore,

$$\Delta W_{\text{total}} = \Delta KE = -150 \text{ J}$$

5 $W_{F, Ff} = 250 \text{ J}$

We can't calculate the work done by non-conservative forces (external forces $-F$ - and friction forces $-F_f$) using the definition of work: $W = F * d * \cos \alpha$, but from the theorem of conservation of mechanical energy we can relate the work done by non-conservative forces to the change in mechanical energy.

Therefore,

$$\Delta W_{F, Ff} = \Delta E = 250 \text{ J}$$

6 $m = 0.8 \text{ kg}$

In this case, we can calculate the mass considering the change in potential energy. We know the angle of the slope and the distance travelled: from these pieces of data we can know the change in altitude:

$$\sin 30^\circ = 0.5 = \frac{\text{altitude}}{\text{distance travelled}}$$
$$\Delta h = h_{\text{final}} - h_{\text{initial}} = 0.5 * 100 \text{ m} = 50 \text{ m}$$

From the change in potential energy, we can determine the mass of the body

$$\Delta PE = 400 \text{ J} = PE_{\text{final}} - PE_{\text{initial}} = m * g * (h_{\text{final}} - h_{\text{initial}})$$
$$\Delta PE = 400 \text{ J} = m * g * \Delta h$$
$$m = \frac{\Delta PE}{g * \Delta h} = \frac{400 \text{ J}}{(10 \text{ m/s}^2) * 50 \text{ m}} = 0.8 \text{ kg}$$

7 $h_{\text{initial}} = 75 \text{ m}$

From the initial potential energy we can get the initial height

$$PE (\text{initial}) = 600 \text{ J} = m * g * h_{\text{initial}}$$
$$h_{\text{initial}} = \frac{PE (\text{initial})}{m * g} = \frac{600 \text{ J}}{8 \text{ N}} = 75 \text{ m}$$

8 $h_{\text{final}} = 125 \text{ m}$

The increase in altitude is 50 m; it means that the final height is 125 m

9 $v_{\text{initial}} = 31.6 \text{ m/s}$

From the value of the initial kinetic energy we can the initial velocity

$$KE_{\text{initial}} = 0.5 * m * v_{\text{initial}}^2 \rightarrow v_{\text{initial}} = \sqrt{\frac{2 * KE_{\text{initial}}}{m}}$$
$$v_{\text{initial}} = 31.6 \text{ m/s}$$

10 $v_{\text{final}} = 25 \text{ m/s}$

From the value of the final kinetic energy we can the final velocity

$$KE_{\text{final}} = 0.5 * m * v_{\text{final}}^2 \rightarrow v_{\text{final}} = \sqrt{\frac{2 * KE_{\text{final}}}{m}}$$
$$v_{\text{final}} = 25 \text{ m/s}$$

11 $F_{\text{net}} = -1.5 \text{ N}$

The distance travelled is 100 m and the total work is -150 J . It means, among other things, that the angle between the force and the direction of motion is 180° . From here, we can determine the net force:

$$W_{\text{total}} = F_{\text{net}} * d * \cos 180^\circ = -F_{\text{net}} * d$$
$$F_{\text{net}} = - \frac{W_{\text{total}}}{d} = \frac{-150 \text{ J}}{100 \text{ m}} = -1.5 \text{ N}$$

12 $a = -1.88 \text{ m/s}^2$

If we apply Newton's second law we get:

$$F_{\text{net}} = m * a \rightarrow a = \frac{F_{\text{net}}}{m} = \frac{-1.5 \text{ N}}{0.8 \text{ kg}} = -1.88 \text{ m/s}^2$$

13 $F_f = 0.69 \text{ N}$

Friction force can be calculated using the following steps:

$$W_y \xrightarrow{N = W_y} N \xrightarrow{F_f = \mu * N} F_f$$

In our case:

$$N = W_y = W * \cos 30^\circ \rightarrow N = 8 \text{ N} * \cos 30^\circ \rightarrow N = 6.9 \text{ N}$$

$$F_f = \mu * N = 0.69 \text{ N}$$

14 $F = 3.19 \text{ N}$

There are different ways to determine the value of the external force. For instance, we can determine it by using this expression:

$$F_{\text{net}} = F - F_f - W_x$$

In our case:

$$W_x = W * \sin 30^\circ = 4 \text{ N}$$

$$-1.5 \text{ N} = F - 0.69 \text{ N} - 4 \text{ N} \rightarrow F = 3.19 \text{ N}$$