



The bodies "A" and "B" start falling at the same time; the initial velocity of "A" is  $v_A = 0$  and the speed (initial) of "B" is  $72 \text{ km/h}$ .

Determine:

- a) the equations of the position vectors (suppose that  $x=0$  along the motion)
- b) the equations of the velocities
- c) the first body that hits the floor
- d) the positions of both when  $t = 2.2 \text{ s}$
- e) their velocities when they hit the floor

Ⓐ  $\vec{r}_A = (50 - 5t^2)\vec{j}$  (m) ...  $y_A = 50 - 5t^2$  (m)

$\vec{r}_B = (80 - 20t - 5t^2)\vec{j}$  (m) ...  $y_B = 80 - 20t - 5t^2$  (m)

$\uparrow v = 72 \frac{\text{km}}{\text{h}} \cdot \frac{1\text{h}}{3600\text{s}} \cdot \frac{1000\text{m}}{1\text{km}} = 20 \frac{\text{m}}{\text{s}}$

Ⓑ  $\vec{r}_A \xrightarrow{\text{differentiation}} \vec{v}_A = -10t\vec{j}$  (m/s)

$\vec{r}_B \xrightarrow{\text{differentiation}} \vec{v}_B = (-20 - 10t)\vec{j}$  (m/s)

Ⓒ "A" body  $\rightarrow$  when it hits the floor  $\rightarrow y_A = 0$

$50 - 5t^2 = 0 \rightarrow t = \sqrt{\frac{50}{5}} = 3.16\text{ s}$

"B" body  $\rightarrow$  when it hits the floor  $\rightarrow y_B = 0$

$80 - 20t - 5t^2 = 0 \rightarrow t^2 + 4t - 16 = 0$

$t = \frac{-4 \pm \sqrt{16 + 64}}{2} = \frac{-4 \pm 8.94}{2}$   $\nearrow$  negative value  
 $\searrow t = 2.47\text{ s}$

"B" body is the first to hit the floor.

Ⓓ  $t = 2.2\text{ s}$

$\hookrightarrow y_A = 50 - 5 \times (2.2)^2 = 25.8\text{ m}$

$\hookrightarrow y_B = 80 - 20 \times 2.2 - 5 \times (2.2)^2 = 11.8\text{ m}$

Ⓔ "A" body

$\hookrightarrow t = 3.16\text{ s} \rightarrow \vec{v}_A = -10 \times 3.16\vec{j}$  (m/s) =  $-31.6\vec{j}$  (m/s)

"B" body

$\hookrightarrow t = 2.47\text{ s} \rightarrow \vec{v}_B = (-20 - 10 \times 2.47)\vec{j}$  (m/s) =  $-44.7\vec{j}$  (m/s)