

Equations of motion

Initial values

Position: x_0, y_0
Velocity: v_{0x}, v_{0y}
Acceleration: a_x, a_y

Position vector: equation

$$\vec{r} = \underbrace{(x_0 + v_{0x} * t + \frac{1}{2} a_x * t^2)}_{\text{"X" component}} \vec{i} + \underbrace{(y_0 + v_{0y} * t + \frac{1}{2} a_y * t^2)}_{\text{"Y" component}} \vec{j}$$

Derivative: rules

$$t^n \xrightarrow{\text{derivative}} n * t^{n-1}$$

$$k * t^n \xrightarrow{\text{derivative}} k * n * t^{n-1}$$

$$k \xrightarrow{\text{derivative}} 0$$

derivative



Velocity – rate of change in position

$$\vec{v} = \underbrace{(v_{0x} + a_x * t)}_{\text{"X" component}} \vec{i} + \underbrace{(v_{0y} + a_y * t)}_{\text{"Y" component}} \vec{j}$$

derivative



Acceleration – rate of change in velocity

$$\vec{a} = a_x \vec{i} + a_y \vec{j}$$

t =

position

at any moment

displacement

change in position
 $\Delta \vec{r} = \vec{r} - \vec{r}_0$

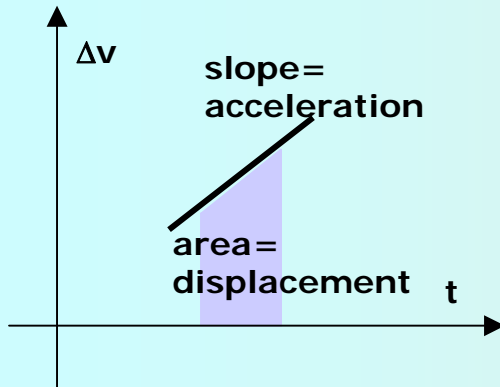
t =

velocity

at any moment

change in velocity

$$\Delta \vec{V} = \vec{V} - \vec{V}_0$$



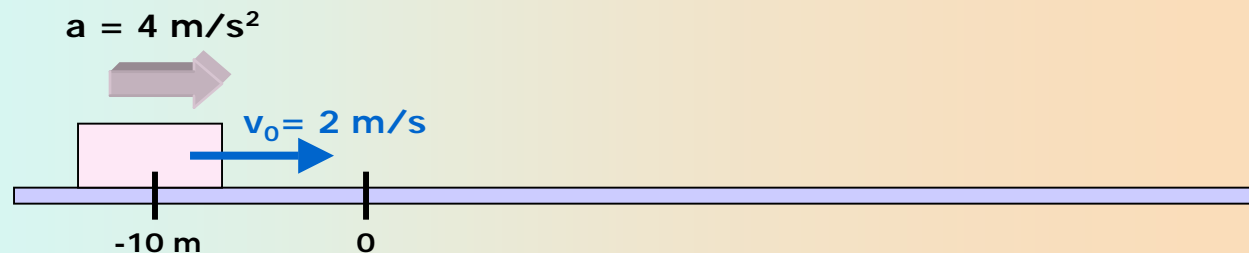
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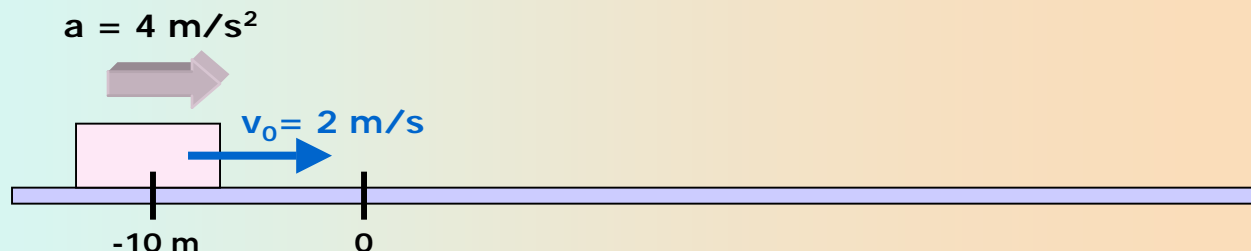
Determine:

- the equation of the position vector
- the displacement between $t=2$ s and $t=4$ s
- the average velocity between $t=2$ s and $t=4$ s
- the equation of the velocity
- the velocities at $t=2$ s and $t=4$ s

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Determine:

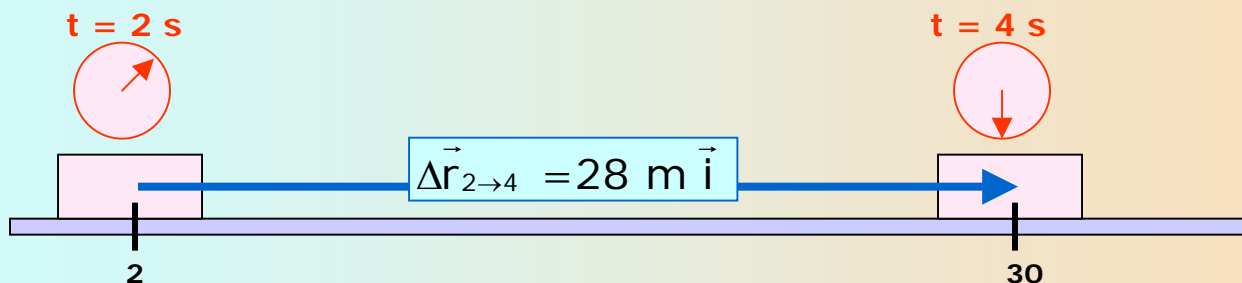
- the equation of the position vector
- the displacement between $t=2 \text{ s}$ and $t=4 \text{ s}$
- the average velocity between $t=2 \text{ s}$ and $t=4 \text{ s}$
- the equation of the velocity
- the velocities at $t=2 \text{ s}$ and $t=4 \text{ s}$

$$\vec{r} = \left(-10 \text{ m} + 2 \frac{\text{m}}{\text{s}} * t + 2 \frac{\text{m}}{\text{s}^2} * t^2 \right) \vec{i}$$

$$\vec{r}_2 = (-10 \text{ m} + 4 \text{ m} + 8 \text{ m}) \vec{i} = 2 \text{ m } \vec{i}$$

$$\vec{r}_4 = (-10 \text{ m} + 8 \text{ m} + 32 \text{ m}) \vec{i} = 30 \text{ m } \vec{i}$$

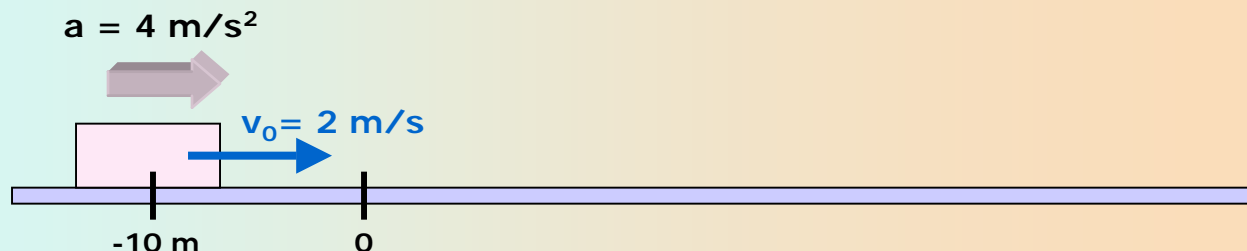
$$\Delta \vec{r}_{2 \rightarrow 4} = \vec{r}_4 - \vec{r}_2 = 30 \text{ m } \vec{i} - 2 \text{ m } \vec{i} = 28 \text{ m } \vec{i}$$



Equations of motion

Initial values

Position: x_0, y_0
Velocity: v_{0x}, v_{0y}
Acceleration: a_x, a_y



Determine:

the average velocity between $t=2$ s and $t=4$ s

- the equation of the velocity
- the velocities at $t=2$ s and $t=4$ s

$$\Delta \vec{r}_{2 \rightarrow 4} = \vec{r}_4 - \vec{r}_2 = 30 \text{ m } \vec{i} - 2 \text{ m } \vec{i} = 28 \text{ m } \vec{i}$$

$$\vec{v} = \frac{\Delta \vec{r}_{2 \rightarrow 4}}{t} = \frac{28 \text{ m } \vec{i}}{4 \text{ s} - 2 \text{ s}} = 14 \frac{\text{m}}{\text{s}} \vec{i}$$

$$\vec{r} = \left(-10 \text{ m} + 2 \frac{\text{m}}{\text{s}} * t + 2 \frac{\text{m}}{\text{s}^2} * t^2 \right) \vec{i}$$

↓ derivative

$$\vec{v} = \left(2 \frac{\text{m}}{\text{s}} + 4 \frac{\text{m}}{\text{s}^2} * t \right) \vec{i}$$

$$\vec{v}_2 = \left(2 \frac{\text{m}}{\text{s}} + 8 \frac{\text{m}}{\text{s}} \right) \vec{i} = 10 \frac{\text{m}}{\text{s}} \vec{i}$$

$$\vec{v}_4 = \left(2 \frac{\text{m}}{\text{s}} + 16 \frac{\text{m}}{\text{s}} \right) \vec{i} = 18 \frac{\text{m}}{\text{s}} \vec{i}$$

