


LIZARDI BHI	2008-09	Gaiak:	PUNTUAZIOA:
Fisika-Kimika	2. ebal.	Dinamika	
2009-03-26		Higidura zirkularra	
Izena:			

- ① a) Indar normalak (N) pisua eta F-ren osagai bertikala orekatu behar ditu:



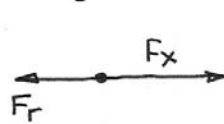
$$N = P + F_y$$

$$P = 12 \text{ Kg} \times 10 \frac{\text{m}}{\text{s}^2} = 120 \text{ N}$$

$$F_y = F \times \sin 30^\circ = 60 \text{ N}$$

$$N = 180 \text{ N}$$

- b) Lehenengo indar totala kalkulatu dugu (higiduraren ardatzean)



$$F_{\text{tot}} = F_x - F_r$$

$$F_x = F \cdot \cos 30^\circ = 103,92 \text{ N}$$

$$F_r = \mu \cdot N = 27 \text{ N}$$

$$F_{\text{tot}} = 76,92 \text{ N}$$

Azelerazioa:

$$a = \frac{F_{\text{tot}}}{m} = \frac{76,92 \text{ N}}{12 \text{ Kg}} \rightarrow a = 6,41 \text{ m/s}^2$$

- c) Zinematikaren ekuazioak erabiliz

$$x = x_0 + v_0 \cdot t + \frac{1}{2} a t^2 \rightarrow 18 \text{ m} = \frac{1}{2} \times 6,41 \frac{\text{m}}{\text{s}^2} \times t^2$$

$$t = \sqrt{\frac{2 \times 18 \text{ m}}{6,41 \text{ m/s}^2}} \rightarrow t = 2,37 \text{ s}$$

Amaierako abiadura:

$$v = v_0 + a t \rightarrow v = 6,41 \frac{\text{m}}{\text{s}^2} \times 2,37 \text{ s} \rightarrow v = 15,19 \frac{\text{m}}{\text{s}}$$

② a) Jarraituko dugun estrategia honela irudika daiteke:

$$\left. \begin{array}{l} a \\ \text{masa} \end{array} \right\} \rightarrow F_{\text{tot}} \rightarrow F_r \rightarrow \mu$$

Indar totala:

$$F_{\text{tot}} = m \times a \rightarrow F_{\text{tot}} = (20 \text{ kg} + 12 \text{ kg}) \times 2,4 \text{ m/s}^2$$

$$\rightarrow F_{\text{tot}} = 76,8 \text{ N}$$

Indar totala jakinik, marruskadura-indarra jakin daiteke:

$$F_{\text{tot}} = P_1 - T_1 + T_2 - F_r \rightarrow F_{\text{tot}} = P_1 - F_r \rightarrow$$

$$\rightarrow 76,8 \text{ N} = 120 \text{ N} - F_r \rightarrow \boxed{F_r = 43,2 \text{ N}}$$

Marruskadura -koefizientea:

$$N = P_2 = 200 \text{ N}$$

$$F_r = \mu \cdot N \rightarrow \mu = \frac{F_r}{N} = \frac{43,2 \text{ N}}{200 \text{ N}} \rightarrow \boxed{\mu = 0,22}$$

b) Tentsioa kalkulatzeko higidari bat isolatuko dugu.



$$F_{\text{tot}} = m \times a \rightarrow P_1 - T_1 = m \times a \rightarrow$$

$$120 \text{ N} - T_1 = 12 \text{ kg} \times 2,4 \text{ m/s}^2 \rightarrow$$

$$120 \text{ N} - T_1 = 28,8 \text{ N} \rightarrow \boxed{T_1 = T_2 = 91,2 \text{ N}}$$

③ a) Abiadura angeluarra periodotik kalkula daiteke:

$$\omega = \frac{2\pi}{T} \rightarrow \omega = \frac{2\pi}{0,15} \rightarrow \boxed{\omega = 62,83 \text{ rad/s}}$$

Unitateak aldatuz:

$$\omega = 62,83 \frac{\text{rad}}{\text{s}} \times \frac{60 \text{ s}}{1 \text{ min}} \times \frac{1 \text{ bira}}{2\pi \text{ rad}} \rightarrow \boxed{\omega = 600 \text{ b.u.}}$$

Abiadura Lineala:

$$v = \omega \times R \rightarrow v = 62,83 \frac{\text{rad}}{\text{s}} \times 2,5 \text{ m} \rightarrow \boxed{v = 157,08 \text{ m/s}}$$

b) Azelerazio normala (zentripetoa)

$$a_c = \frac{v^2}{R} \rightarrow \boxed{a_c = 9869,65 \text{ m/s}^2}$$

c) Higidazaren masa:

$$F = m \times a_c \rightarrow m = \frac{F}{a_c} \rightarrow m = \frac{280 \text{ N}}{9869,65 \text{ m/s}^2}$$

$$\rightarrow \boxed{m = 28,37 \text{ g}}$$

d) Higiduraren maiztasuna

$$f = \frac{1}{T} \rightarrow f = \frac{1}{0,15} \rightarrow \boxed{f = 10 \text{ Hz}}$$

- ④ a) Higiduraren noranzkoa erabakitzeke bi indar hauek alderatu behar ditugu: P_1 eta P_{2x}

$$\left. \begin{aligned} P_1 &= m_1 \times g = 80 \text{ N} \\ P_{2x} &= P_2 \times \sin 30^\circ = 50 \text{ N} \end{aligned} \right\} \text{ Sistemak, honela mugitzeko joera du:}$$

- b) Indar normalaren (N) balioa:

$$N = P_{2y} \rightarrow P_{2y} = P_2 \times \cos 30^\circ \rightarrow \boxed{N = 86,6 \text{ N}}$$

Marruskadura-indarra (F_r):

$$F_r = \mu \cdot N = 0,05 \times 86,6 \text{ N} \rightarrow \boxed{F_r = 4,33 \text{ N}}$$

- c) Azelerazioa:

$$F_{\text{tot}} = m \times a \rightarrow F_{\text{tot}} = P_1 - P_{2x} - F_r = 25,67 \text{ N}$$

$$a = \frac{F_{\text{tot}}}{m} \rightarrow a = \frac{25,67 \text{ N}}{18 \text{ kg}} \rightarrow \boxed{a = 1,43 \text{ m/s}^2}$$

- d) Tentsioa

$$\begin{array}{l} \uparrow T_1 \\ \bullet \\ \downarrow P_1 \end{array} \quad \begin{aligned} F_{\text{tot}} &= m \times a \rightarrow P_1 - T_1 = m \times a \rightarrow \\ 80 \text{ N} - T_1 &= 8 \text{ kg} \times 1,43 \text{ m/s}^2 \rightarrow \\ 80 \text{ N} - T_1 &= 11,44 \text{ N} \rightarrow \boxed{T_1 = T_2 = 68,56 \text{ N}} \end{aligned}$$